

Čiste' derivace

$$f(x) = \ln \frac{1 + \sqrt{x^4 + 1}}{x^2}$$

$$f'(x) = \frac{1}{\frac{1 + \sqrt{x^4 + 1}}{x^2}} \cdot \frac{\frac{1}{2\sqrt{x^4 + 1}} \cdot 4x^3 \cdot x^2 - (1 + \sqrt{x^4 + 1}) \cdot 2x}{x^4} =$$

$$= \frac{x^2}{1 + \sqrt{x^4 + 1}} \cdot \frac{\frac{2x^5}{\sqrt{x^4 + 1}} - 2x(1 + \sqrt{x^4 + 1})}{x^4} =$$

$$= \frac{1}{1 + \sqrt{x^4 + 1}} \cdot \frac{\frac{2x^5}{\sqrt{x^4 + 1}} - 2x(1 + \sqrt{x^4 + 1})}{x^2} = \frac{1}{1 + \sqrt{x^4 + 1}} \cdot \left( \frac{2x^5}{\sqrt{x^4 + 1}} \cdot \frac{1}{x^2} - \right.$$

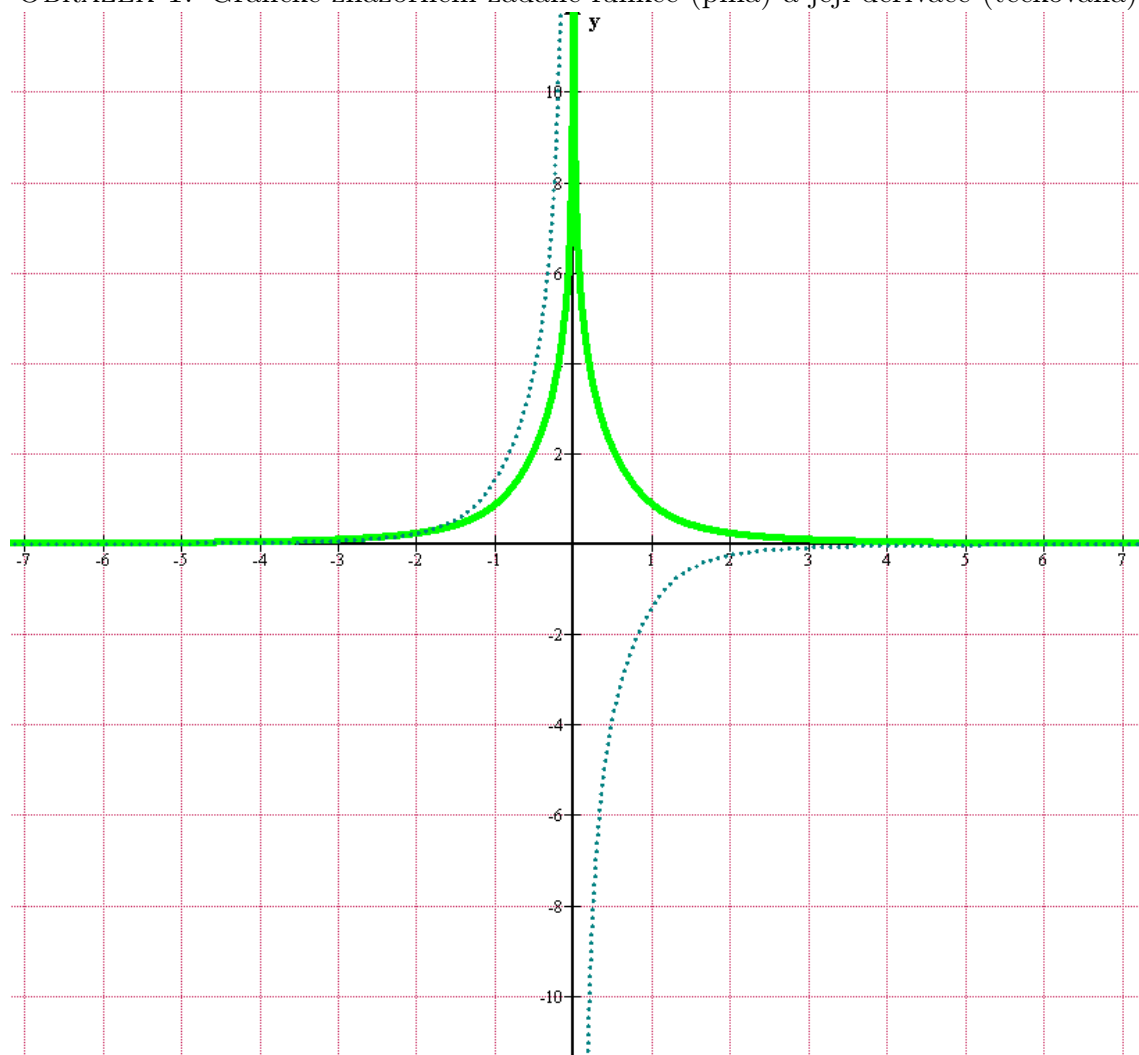
$$\left. - \frac{2x(1 + \sqrt{x^4 + 1})}{x^2} \right) = \frac{1}{1 + \sqrt{x^4 + 1}} \cdot \left( \frac{2x^3}{\sqrt{x^4 + 1}} - \frac{2(1 + \sqrt{x^4 + 1})}{x} \right) =$$

$$= \frac{1}{1 + \sqrt{x^4 + 1}} \cdot \frac{2x^3 - 2(1 + \sqrt{x^4 + 1}) \cdot \sqrt{x^4 + 1}}{x \sqrt{x^4 + 1}} = \frac{1}{1 + \sqrt{x^4 + 1}} \cdot \frac{2x^3 - 2\sqrt{x^4 + 1} - 2(x^4 + 1)}{x \cdot \sqrt{x^4 + 1}} =$$

$$= \frac{1}{1 + \sqrt{x^4 + 1}} \cdot \frac{2x^3 - 2\sqrt{x^4 + 1} - 2x^4 - 2}{x \cdot \sqrt{x^4 + 1}} = \frac{1}{1 + \sqrt{x^4 + 1}} \cdot \frac{-2(\sqrt{x^4 + 1} + 1)}{x \sqrt{x^4 + 1}} =$$

$$= \frac{-2}{x \cdot \sqrt{x^4 + 1}}$$

OBRÁZEK 1. Grafické znázornění zadané funkce (plná) a její derivace (tečkovaná)



Zdroj: program Graph